

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATICS			0580/43
Paper 4 (Extended)			May/June 2017
			2 hours 30 minutes
Candidates answer or	the Question Paper.		
Additional Materials:	Electronic calculator Tracing paper (optional)	Geometrical instruments	

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.

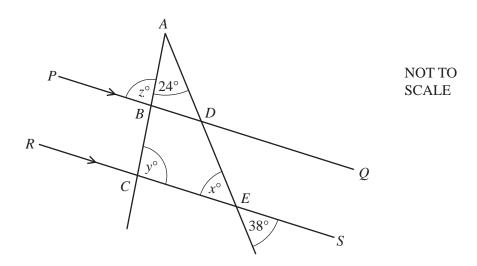


(a)	In 2	016, a company sold 9600 cars, correct to the nearest hundred	d.
	(i)	Write down the lower bound for the number of cars sold.	
			[1]
	(ii)	The average profit on each car sold was \$2430, correct to the	e nearest \$10.
		Calculate the lower bound for the total profit. Write down the exact answer.	
			\$[2]
	(iii)	Write your answer to part (a)(ii) correct to 4 significant figure	ures.
			\$[1]
	(iv)	Write your answer to part (a)(iii) in standard form.	
			\$[1]
(b)		April, the number of cars sold was 546. s was an increase of 5% on the number of cars sold in March.	
	Calo	culate the number of cars sold in March.	
			[3]

(c)	The price of a new car grows exponentially by 3% per year.
	A new car has a price of \$3000 in 2013.

Find the price of a new car 4 years later.

2 (a)

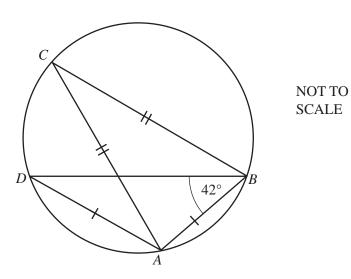


PQ is parallel to RS. ABC and ADE are straight lines.

Find the values of x, y and z.

х	=	•••	•••	••	• •	•	•	••	••	•	••	• •	•	••	•	••	•	 • •	•	•	• •	•	• •		•	• •	••	•	••	•		
у	=		•••	•••		•	•		••		••		•	••		••	•	 	•	•								•				
7	=																	 										_		_	[3	3

(b)

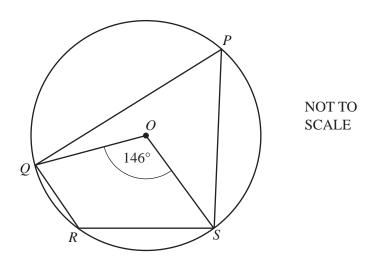


The points A, B, C and D lie on the circumference of the circle. AB = AD, AC = BC and angle $ABD = 42^{\circ}$.

Find angle *CAB*.

Angle *CAB* =[3]

(c)



The points P, Q, R and S lie on the circumference of the circle, centre O. Angle $QOS = 146^{\circ}$.

Find angle *QRS*.

Angle *QRS* =[2]

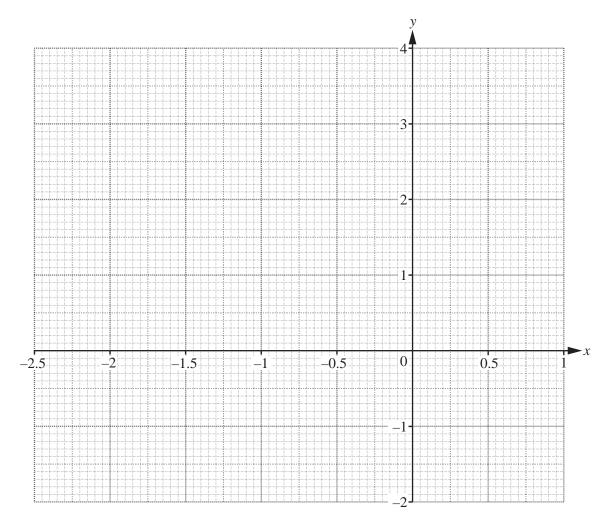
3 The table shows some values for $y = 2x^3 + 4x^2$.

х	-2.2	-2	-1.5	-1	-0.5	0	0.5	0.8
у	-1.94				0.75	0		3.58

(a) Complete the table.

[4]

(b) Draw the graph of $y = 2x^3 + 4x^2$ for $-2.2 \le x \le 0.8$.



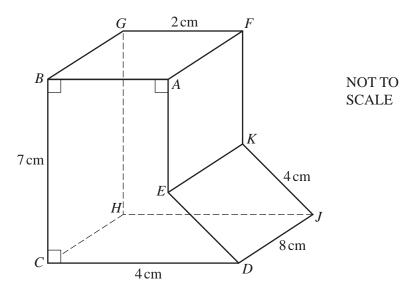
[4]

(c) Find the number of solutions to the equation $2x^3 + 4x^2 = 3$.

.....[1]

(d)	(i)	The equation $2x^3 + 4x^2 - x = 1$ can be solved by drawing a straight line on the grid.
		Write down the equation of this straight line.
		<i>y</i> =[1]
	(ii)	Use your graph to solve the equation $2x^3 + 4x^2 - x = 1$.
		$x = \dots $ or $x = \dots $ or $x = \dots $ [3]
(e)	The	tangent to the graph of $y = 2x^3 + 4x^2$ has a negative gradient when $x = k$.
(e)		tangent to the graph of $y = 2x^3 + 4x^2$ has a negative gradient when $x = k$. Applete the inequality for k .
(e)		
(e)		
(e)		

4 (a) The diagram shows a solid metal prism with cross section ABCDE.



(i) Calculate the area of the cross section ABCDE.

2.	
cm ²	6

(ii) The prism is of length 8 cm.

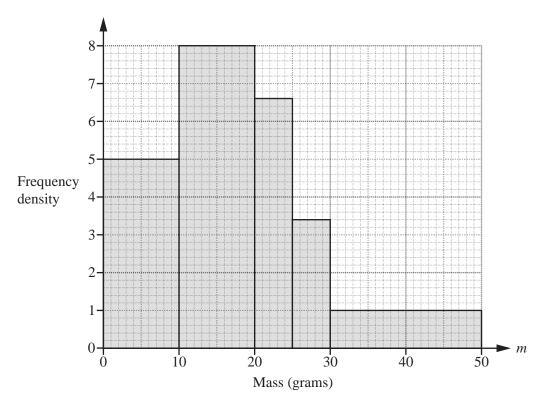
Calculate the volume of the prism.

.....cm³ [1]

(b)	A cy	vlinder of length 13 cm has volume 280 cm ³ .
	(i)	Calculate the radius of the cylinder.
		···· [2]
	(;;)	The cylinder is pleased in a hear that is a cybe of side 14 cm.
	(ii)	The cylinder is placed in a box that is a cube of side 14 cm.
		Calculate the percentage of the volume of the box that is occupied by the cylinder.
		04 [2]
		% [3]

5 (a) Haroon has 200 letters to post.

The histogram shows information about the masses, m grams, of the letters.



(i) Complete the frequency table for the 200 letters.

Mass (m grams)	$0 < m \le 10$	$10 < m \le 20$	$20 < m \le 25$	$25 < m \leqslant 30$	30 < m ≤ 50
Frequency	50			17	

[3]

(ii) Calculate an estimate of the mean mass.

..... g [4]

(b) Haroon has 15 parcels to post.

The table shows information about the sizes of these parcels.

Size	Small	Large
Frequency	9	6

Two parcels are selected at random.

Find the probability that

(i) both parcels are large,

[2	2		
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(ii) one parcel is small and the other is large.

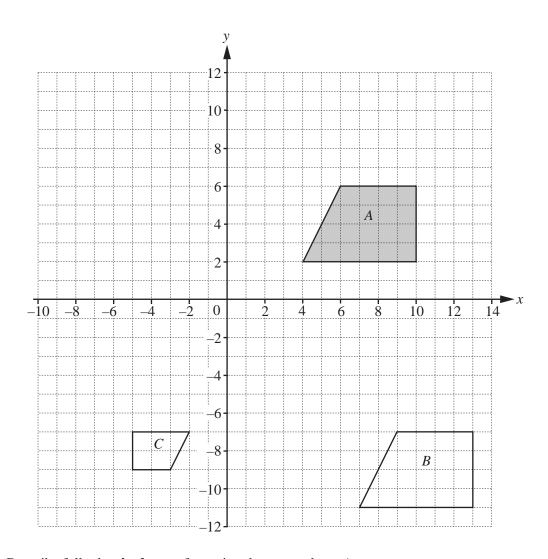
.....[3]

(c) The probability that a parcel arrives late is $\frac{3}{80}$. 4000 parcels are posted.

Calculate an estimate of the number of parcels expected to arrive late.

.....[1]

6



(a) Describe fully the **single** transformation that maps shape A onto

	(i)	shape B ,	
			[2]
	(ii)	shape C.	
			[3]
(b)	Drav	w the image of shape A after rotation through 90° anticlockwise about the point $(3, -1)$.	[2]
(c)		w the image of shape A after reflection in $y = 1$.	[2]
(d)	Desc	cribe fully the single transformation represented by the matrix $\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$.	
	•••••		

7	(a)	Solve the simultaneous equations.
		You must show all your working.

your working.
$$2x + 3y = 11$$
$$3x - 5y = -50$$

<i>x</i> =	
y =[4	-]

(b)
$$x^2 - 12x + a = (x+b)^2$$

Find the value of a and the value of b.



(c) Write as a single fraction in its simplest form.

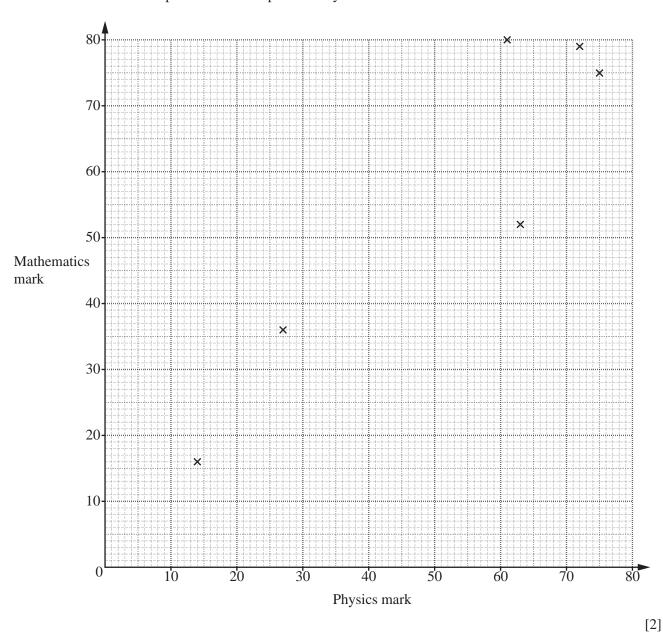
$$\frac{x}{2x-5} + \frac{3x+2}{x-1}$$

8 (a) The table shows the marks gained by 10 students in their physics test and their mathematics test.

Physics mark	63	61	14	27	72	75	44	40	28	50
Mathematics mark	52	80	16	36	79	75	51	35	24	63

(i) Complete the scatter diagram below.

The first six points have been plotted for you.



(ii) What type of correlation is shown in the scatter diagram?

.....[1]

(b) The marks of 30 students in a spelling test are shown in the table below.

Mark	0	1	2	3	4	5
Frequency	2	4	5	5	6	8

Find the mean, median, mode and range of these marks.

Mean =	•••••	 	••
Median =	•••••	 	···
Mode =		 	·
Range =		 	[7]

(c) The table shows the marks gained by some students in their English test.

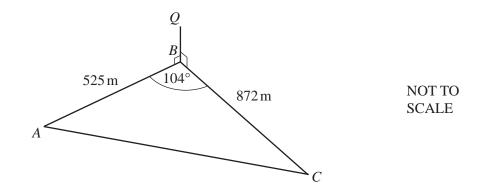
Mark	52	75	91
Number of students	X	45	11

The mean mark for these students is 70.3.

Find the value of x.

x =.....[3]

9



ABC is a triangular field on horizontal ground. There is a vertical pole BQ at B. AB = 525 m, BC = 872 m and angle $ABC = 104^{\circ}$.

(ัล) Use	the	cosine	rule	to	calculate	the	distance	AC
١	u	, Osc	uic	COSITIC	ruic	w	carcurate	uic	distance	110

$AC = \dots m [4]$

(b) The angle of elevation of Q from C is 1.0°.

Showing all your working, calculate the angle of elevation of Q from A.

.....[4]

(c)	(i)	Calculate the area of the field.	
		$\dots \dots $	m^2 [2]
	(ii)	The field is drawn on a map with the scale 1:20000.	cale 1:20000.
		Calculate the area of the field on the map in cm ² .	nap in cm ² .
		\cdots cm^2	cm ² [2]

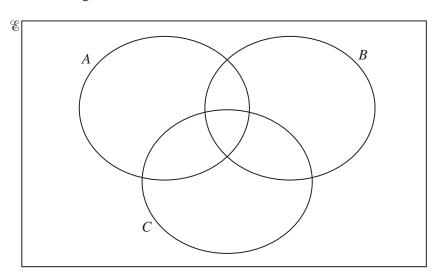
10 $\mathscr{E} = \{21, 22, 23, 24, 25, 26, 27, 28, 29, 30\}$

 $A = \{ x : x \text{ is a multiple of 3} \}$

 $B = \{ x : x \text{ is prime} \}$

 $C = \{ x : x \le 25 \}$

(a) Complete the Venn diagram.



[4]

(b) Use set notation to complete the statements.

(i)	26 R	[1]	1
(1)	20 D	1	1

(ii)
$$A \cap B = \dots$$
 [1]

(c) List the elements of $B \cup (C \cap A)$.

.....[2]

(d) Find

(i) n(C),

.....[1]

(ii) $n(B' \cup (B \cap C))$.

.....[1]

(e) $(A \cap C)$ is a subset of $(A \cup C)$.

Complete this statement using set notation.

 $(A \cap C)$ $(A \cup C)$ [1]

11 The table shows the first four terms in sequences A, B, C and D.

Complete the table.

Sequence	1st term	2nd term	3rd term	4th term	5th term	<i>n</i> th term
A	16	25	36	49		
В	5	8	11	14		
С	11	17	25	35		
D	$\frac{3}{2}$	$\frac{4}{3}$	<u>5</u> 4	$\frac{6}{5}$		

[12]

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